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23 1 Abstract

24 To better understand the effect and influence of spatial density of ground motion
25 predictions, we attempted to combine data from multiple seismic networks from the same
26 region and compare intensity predictions with and without new seismological networks. The
27 U-Net neural network architecture is used as a ground motion model that predicts the mean
28 and standard deviation of a target intensity measure (IM, PGA) in the form of maps. The
29 U-Net can interpolate the intensity measures between the observation points inherently and
30 we here try to analyse the effect of spatial density in this interpolation by using multiple
31 networks. Kanto basin in Japan is selected for this study due to the availability of dense
32 seismic networks within the basin and we integrated the KIK-net and the MeSO-net networks
33 within the basin for this study. The results show that the errors and the uncertainty levels
34 between the predictions and the observations at the interpolated sites slightly decreased
35 after adding an additional network for the training process, but the statistical significance is
36 questionable. However, more networks or more observations per station are required to be
37 integrated and trained within the same region to analyse and validate our results.

38 2 Introduction

39 Over the last few decades, a large number of ground-motion models (GMMs) have
40 been developed for use in seismic hazard and risk applications all over the world. GMMs
41 define the ground motion field in terms of earthquake source characteristics (e.g., magnitude,
42 fault mechanism), wave propagation (e.g., epicentral distance), and site effects (e.g., site class
43 or *VS30*) to predict specific intensity measures (IM). For various tectonic regions, tens or
44 even hundreds of candidate models are available due to the intricacy of the earthquake
45 process, wave propagation, and site effects; examples can be found in Douglas (2020). These
46 models represent the distribution of ground-motion in terms median intensity measure and
47 its standard deviation (Strasser et al. 2009).

48 The U-Net neural network architecture has been used recently as a ground motion
49 model that predicts the mean and standard deviation of a target intensity measure (IM,
50 PGA) in the form of maps (Lilienkamp et al. 2022). The U-Net, it learns the relationship
51 between predictive parameters and target parameters using a large number of instances
52 that are presented to train the neural network, just like all supervised learning techniques.
53 In ground-motion modelling, the target parameter is a ground-motion IM, which may be
54 deduced from predictive factors such as the moment magnitude M_w and the hypocentral
55 distance r_{hyp} . The U-Net neural network architecture has been used recently as a ground
56 motion model that predicts the mean and standard deviation of a target intensity measure
57 (IM, PGA) in the form of maps (Lilienkamp et al. 2022). The U-Net can interpolate the
58 intensity measures between the observation points inherently and we here try to analyze
59 the effect of spatial density of observation points in this interpolation by using multiple
60 seismological networks (e.g. MeSO-NET).

61 To better understand the effect and influence of arrays spatial density on ground mo-
62 tion predictions, we attempted to combine data from multiple seismological networks from
63 the same region and compare intensity predictions with and without new seismological sta-
64 tions. The relative surface fault motion for recording stations situated on either side of a
65 causative fault, soil liquefaction, landslides, and the general transmission of the waves from
66 the source through the various earth strata to the ground surface can all contribute to the spa-
67 tial variability in seismic ground motions (Zerva & Zervas 2002). This architecture’s inherent
68 capacity to process data in the form of 2D arrays (maps) makes it particularly appealing for
69 ground-motion modeling, as it allows for native operations on map data, which preserves the
70 underlying spatial distribution of ground-motion observations (Lilienkamp et al. 2022). This
71 visualization method provides a clear picture of how spatial density of observation points
72 affects ground motion predictions. This spatial variation of seismic ground motions has
73 started being analyzed after the installation of these kinds of dense instrument arrays. The
74 sensors used for these arrays are costly and also time-consuming, hence studies are required

75 to really understand the effect of these arrays and to find an optimal array that minimises
76 the error in model predictions. In this study, we focus on the effect of spatial density of
77 the stations in the intensity predictions and the associated uncertainties by integrating data
78 from different seismological networks.

79 In this report, we use the U-net architecture to understand the relation between
80 the IM (here PGA) and predictive parameters in the Kanto basin using a subset of the
81 Kiban–Kyoshin (KiK-net) dataset. We then look at how integrating two datasets from the
82 same region (Kanto Basin) - the KiK-net and the highly dense Metropolitan Seismic Observa-
83 tion network (MeSO-net), affects the interpolation of IMs and their associated uncertainties
84 between the observation points. Here we work with the PGA values while the original work
85 of (Lilienkamp et al. 2022) focused and tested only for SA(T=1s).

86 **3 Data Used**

87 Kanto basin in Japan is selected for this specific study due to the high-density seis-
88 mic networks available within the basin. The basin has KiK- et stations, MeSO-net stations
89 (Sakai & Hirata 2009), K-net stations (National Research Institute for Earth Science and
90 Disaster Resilience, 2019) and some QuakeSaver devices are also installed within some build-
91 ings in the region.

92 We are primarily interested in determining and analyzing the difference in the uncer-
93 tainty in U-Net’s interpolation of intensity measures between station locations when data
94 from numerous networks is used instead of a single network, hence, the goal of our study
95 necessitates the use of high-density networks of this type. We focus on two networks in this
96 report, i.e, KiK-net and MeSO-net as shown in Figure 1. Both KiK-net and MeSO-net are
97 operated by National Research Institute for Earth Science and Disaster Resilience, NIED
98 (2019).

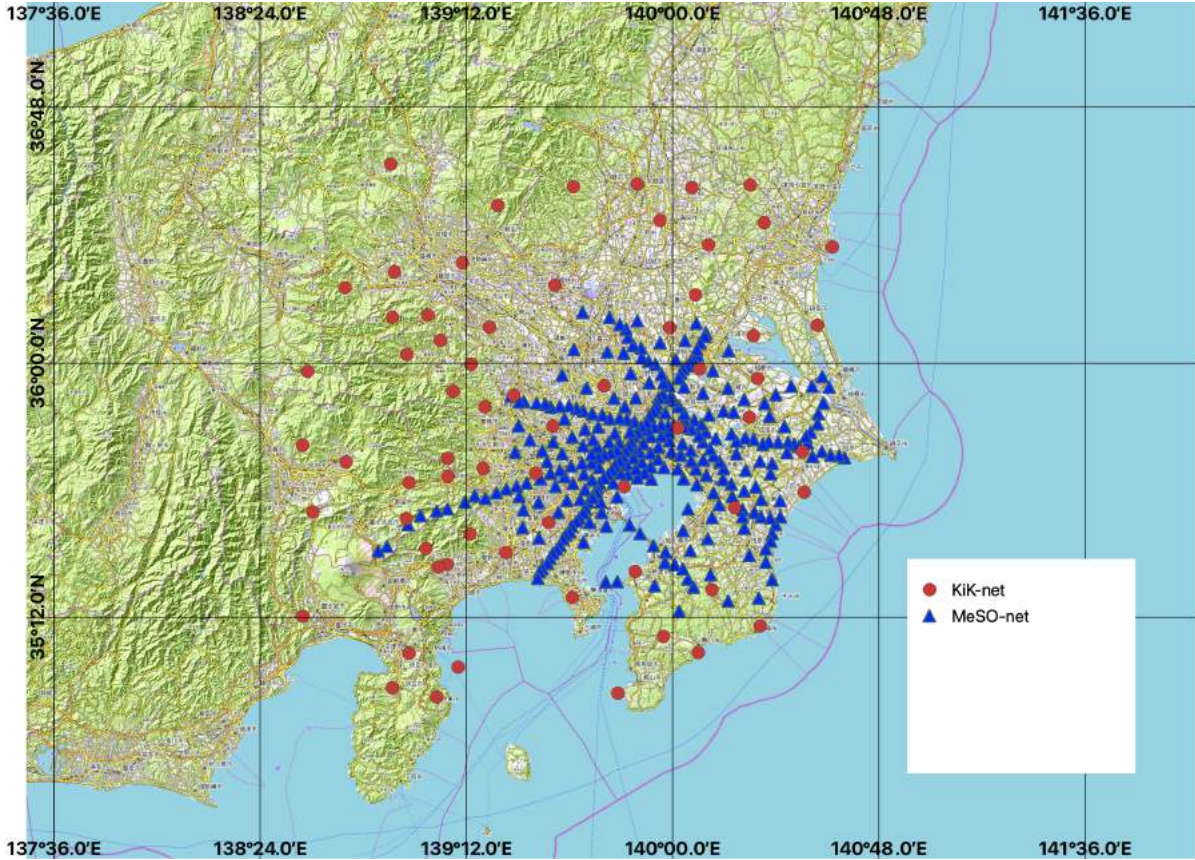


Figure 1: *KiK-net and MeSO-net station coverage in the Kanto Basin. Blue triangles indicate the MeSO-net locations (highly dense) and the red circles are the KiK-net station locations.*

99 3.1 KiK-net dataset

100 KiK-net consists of pairs of strong-motion seismographs installed in a borehole and
 101 on the ground surface. Here, we used exactly the same dataset given by Bahrapouri et al.
 102 (2021) comprising both surface and borehole sensors. We downloaded the processed data by
 103 Bahrapouri et al. (2021). The database utilized in this study comprises all earthquakes
 104 with a magnitude greater than three that were recorded on the KiK-net website between
 105 1996 and the end of 2017 and used by Bahrapouri et al. (2021), Lilienkamp et al. (2022).
 106 We used 46,191 records from 2864 events recorded at 65 different stations. The selected KiK-
 107 net stations have an average inter-station distance of about 94 km. As our target intensity,

108 we used the geometric mean of the PGA values. The distribution of the dataset is given in
 109 Figure 2.

110 3.2 MeSO-net dataset

111 MeSO-net is made up of around 300 observation stations in the Tokyo metropolitan
 112 region, as illustrated in Figure 1 (blue triangles). These stations are made up of five dense
 113 linear arrays spaced around 2 to 3 km apart and a sparser distribution with a radius of about
 114 80 km spaced roughly 4 to 10 km apart. This network is highly dense compared to the inter-
 115 station distance of KiK-net stations. MeSO-net stations (three-component accelerometer)
 116 are located at the bottom of 20 m deep boreholes. This data is converted to correspond to
 117 the intensity at the ground surface according to Aoi et al. (2021) by adding 0.5 to $\log(\text{PGA})$
 118 at all stations at all stations (accounting for the free surface factor).

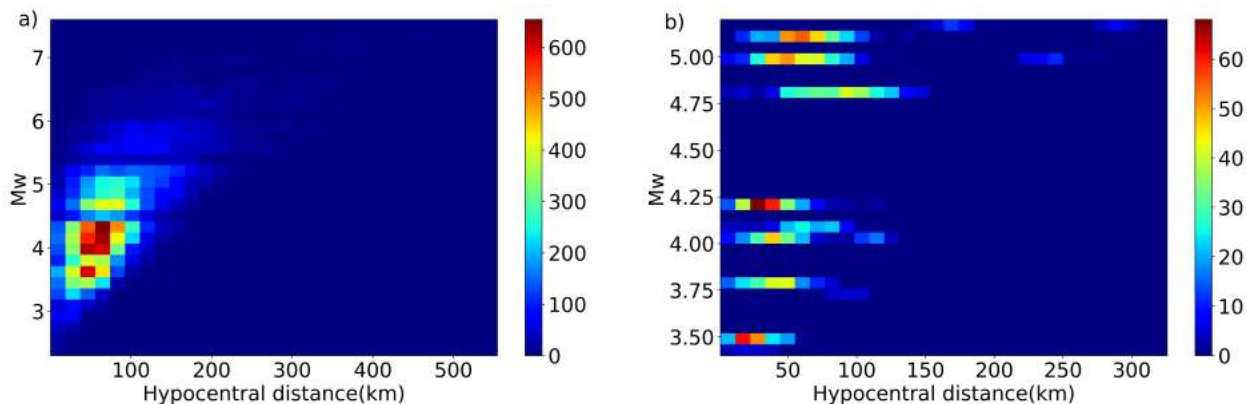


Figure 2: Data from Kanto basin used for this study. Hit counts computed for the data distribution, dividing the distance range into 20 equally spaced bins over the hypocentral distance and the moment magnitude (M_w). a) KiK-net dataset b) MeSO-net dataset.

119 The MeSO-Net waveform data is downloaded from the National Research Institute
 120 for Earth Science and Disaster Resilience (NIED) website. The website provides the data
 121 from 2021 and 2022. A total of 1921 recordings are obtained from 19 events recorded at
 122 300 different stations in the Kanto Basin. Figure 2 depicts the data distribution of both
 123 networks - the KiK-net and the MeSO-net. Data used from MeSO-net for this study is only

124 available from a limited time period.

125 **4 Methodology**

126 **4.1 The U-net architecture**

127 The U-net neural network architecture (Ronneberger et al. 2015) is the central com-
128 ponent of our methodology, as it can offer us with a fully non-ergodic and data-driven GMM.
129 Lilienkamp et al. (2022) introduced this to the ground motion modelling area, and the paper
130 tests the U-net as a GMM and explains how it can work as a GMM. Figure 2 illustrates this.
131 The input parameters are the nine maps shown in the figure, i.e, the latitude and longitude
132 of the event, the depth, magnitude, the coordinates of each pixel in the input layer (572
133 $\times 572$ pixels), the hypocentral distance and the depth to seismic bedrock. The output will
134 be the mean, \hat{y} and variance, σ^2 of the IM. The valid convolution operations reduces the
135 resolution of the output features is to 388×388 compared to that of the input features.
136 Through a series of instances and iterations, the U-net algorithm learns the link between the
137 input parameters and the output. Detailed information on the neural networks can be found
138 in LeCun et al. (2015). The U-net is particularly useful for ground motion modelling since
139 it is designed to process data in the form of 2D arrays, or maps. The U-Net’s predictive
140 parameters are provided in the form of a stack of maps spanning a predefined area, and the
141 U-Net is trained to provide estimates of the target IM’s mean and variance. The negative
142 log-likelihood is considered as the model error or the loss between the model outputs and
143 the observations for an event with N observations. The loss is iteratively minimized using
144 the gradient descent algorithm Adam (Da 2014), with the gradient effectively implemented
145 using backpropagation (Rumelhart et al. 1986).

146 After one cycle (epoch) of training using all of the training data, the neural network’s
147 training is tested using the validation dataset. After a given number of epochs, the loss
148 on the validation dataset does not decrease any further, indicating that the training is
149 complete and the U-Net may now be used as a GMM. Instead of point-wise observations,

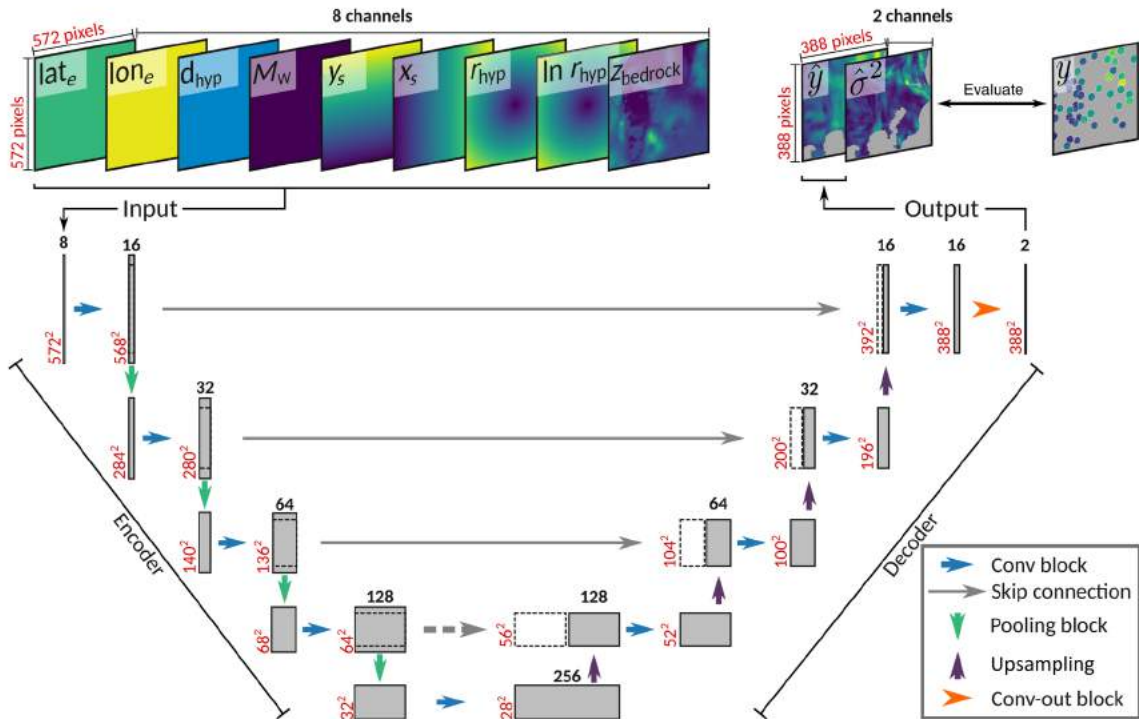


Figure 3: This study’s U-Net architecture [Figure from Lilienkamp et al. (2022)]. The U-Net receives the predictive parameters for a single earthquake as input in the form of a stack of maps. The input is processed, and the intensity measure (IM) mean \hat{y} and variance $\hat{\sigma}^2$ estimators are provided as output. Lat_e , lon_e , and d_{hyp} are the latitude, longitude, and depth of the event hypocenter, respectively. M_w is the moment magnitude, x_s and y_s are the coordinates of each pixel in the input layer, r_{hyp} is the hypocentral distance, and $z_{bedrock}$ is the depth to seismic bedrock. This figure is described in more detail in (Lilienkamp et al. 2022). This figure is based on the first figure of Ronneberger et al. (2015).

150 the U-net predictions are continuous maps. This means that the loss function is generated
 151 first at sites where actual observations are available, and then the U-Net interpolates the
 152 learned attenuation relation from those locations. The data was separated into training and
 153 validation events using the same training technique as (Lilienkamp et al. 2022), i.e.,

- 154 • The data were divided into training and validation events. All events occurring up to
 155 2015 are used for training, while those occurring 2015 and onwards are considered
 156 validation events.

- 157 • Stations are divided into a number of chunks at random (N_{chu}) - for each station chunk,
 158 one U-net is trained (the selected station chunk is excluded from training in order to
 159 be used for validation after training).
- 160 • The U-net is run N_{init} times to quantify the variability caused by random coefficient
 161 initialization. The final predictions for the mean and variance of the target IM for the
 162 event e (\hat{Y}_e and the $\hat{\Sigma}_e$, respectively), are obtained by ensemble averaging the mean and
 163 variance predictions of the individual U-Nets (\hat{y}_e^{ij} and the $\hat{\sigma}_e^{ij}$, respectively). The total
 164 number of U-Nets will be, $N_U = N_{chu} * N_{init}$ and the mean and variance of the final
 165 predicted IM according to the law of total expectation and the law of total variance
 166 (Blitzstein & Hwang 2015) for an event will be

$$\hat{Y}_e = 1/N_U \sum_{i=1}^{N_{chu}} \sum_{j=1}^{N_{init}} \hat{y}_e^{ij} \quad (1)$$

167

$$\hat{\Sigma}_e^2 = 1/N_U \sum_{i=1}^{N_{chu}} \sum_{j=1}^{N_{init}} [\hat{\sigma}_e^{ij^2} + \hat{y}_e^{ij^2}] - \hat{Y}_e^2 \quad (2)$$

168 The U-Net learns the site amplification as a function of the coordinates of the station
 169 location, source-location specific variability from the event latitude and longitude, and path-
 170 specific amplification from the coordinates of each pixel and from the latitude and longitude
 171 of the events. We initially analyzed the U-net findings using only the KiK-net dataset, then
 172 trained the U-net using both the KiK-net and MeSO-net datasets to see how the results
 173 differ in terms of increasing the number of observation sites between the existing ones (the
 174 KiK-net stations).

175 4.2 U-Net training with different seismological networks - Kanto Basin

176 We started (the first stage) of the U-Net training with the KiK-net strong-motion
 177 dataset by (Bahrapouri et al. 2021) for peak ground acceleration (PGA) measurements. All
 178 events occurring up to 2015 are used for training, while those occurring 2015 and onwards are

179 considered validation events. The 65 stations are separated into 5 chunks, with each chunk
180 receiving a random selection of the stations and 10 random initializations. We proceed with
181 the inclusion of the MeSO-net dataset after obtaining the predicted PGA values with the
182 KiK-net dataset. We use both the KiK-net and MeSO-net recordings for the training in
183 this stage. For the training phase, both the events occurring before 2015 (only KiK-net)
184 and after 2020 (only MeSO-net events) are evaluated. The validation events are set as the
185 same sets we used in the first step in order to understand the changes after adding a new
186 dense network (MeSO-net) with the KiK-net data in training process, i.e, the same KIK-net
187 station chunks are used for validation of interpolated IM values. A summary of this is shown
188 in the flowchart.(Figure 4)

189 5 Results and Discussion

190 5.1 Interpolation Quality

191 We first analyse the effect in the interpolation of IMs when arrays of stations (MeSO-
192 net) are integrated to the KiK-net dataset in the same region, Kanto basin. As we have
193 discussed earlier the U-net automatically interpolates the learned relation from the obser-
194 vation locations across the output area and we study the quality of this interpolation using
195 the partial ensemble estimators, $\hat{\mathcal{Y}}^i$, for which the i th station chunk was not used during
196 training. Averaging over the subsets of U-Nets that share the same i th station validation
197 chunk yields partial ensemble estimators. Lilienkamp et al. (2022) evaluated and classified
198 these partial ensemble estimators in four different ways to understand the performance of
199 U-Net at the interpolated sites and we use the same technique to assess the effect of spatial
200 density in the interpolation. The four different categories are (1) training events recorded
201 on training stations, (2) validation events recorded on training stations, (3) training events
202 recorded on validation stations, and (4) validation events recorded on validation stations.
203 We average the root mean square error (rmse) between the observations and predictions
204 (Ln) over the five station chunks $\hat{\mathcal{Y}}^i$. The average of the rmse values using only the KiK-net

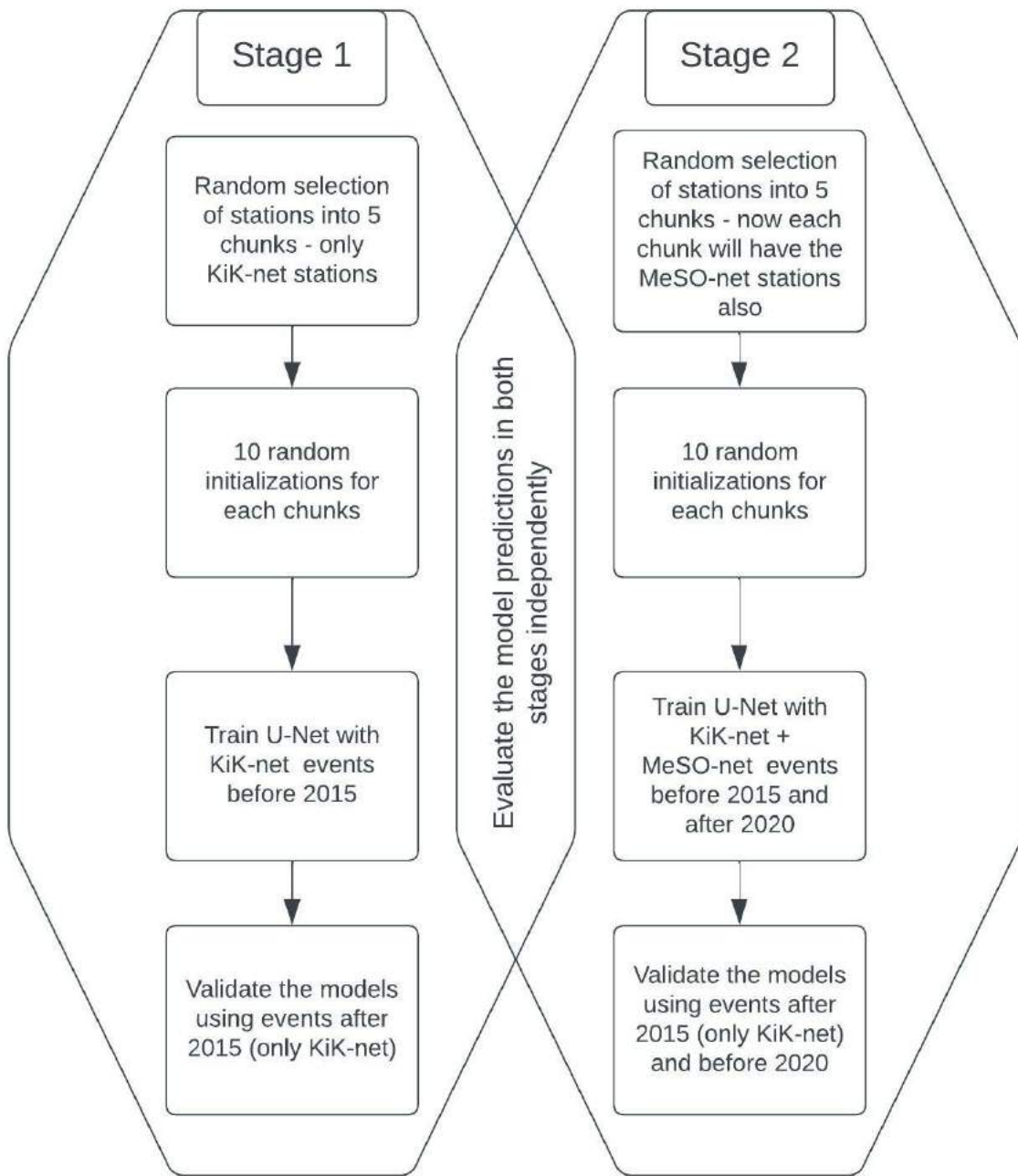


Figure 4: Flowchart describing the process used in this study.

205 stations is given in Table 1. The rmse values are larger when using the validation stations,
 206 as seen in the table, because these predictions from the validation stations have additional
 207 errors owing to interpolation. The training events and the training stations will have the
 208 smallest rmse values as those observations are the ones used for training.

Table 1: Average Root Mean Square Errors \pm 1 Standard Deviation between Observations and Predictions of the Five Partial Ensemble Estimators using only KiK-net.

Configuration	Rmse
Training stations/training events	0.432 ± 0.007
Training stations/Validation events	0.496 ± 0.005
Validation stations/training events	0.871 ± 0.104
Validation stations/validation events	0.854 ± 0.090

Table 2: Average Root Mean Square Errors \pm 1 Standard Deviation between Observations and Predictions of the Five Partial Ensemble Estimators using both KiKnet and MeSO-net.

Configuration	Rmse
Training stations/training events	0.429 ± 0.007
Training stations/Validation events	0.494 ± 0.005
Validation stations/training events	0.865 ± 0.086
Validation stations/validation events	0.841 ± 0.080

209 The rmses in Ln units are then analyzed using both the KiK-net and MeSO-net
 210 stations to see how integrating more stations affects the results. The validation stations
 211 rmses with and without the MeSO-net stations are of particular interest because they are the
 212 predictions with the interpolation error. The average of the rmses between the observations
 213 and predictions over the five $\hat{\mathcal{Y}}^i$ using both the networks is given in Table 2. As shown in
 214 the table the rmse values decreased in all the four configurations. The change of rmses are
 215 within the standard deviation provided in the tables for all the four combinations, which
 216 may provide the idea that the changes are not that significant. Due to the small number of
 217 MeSO-net records compared to KIK-net records, the influence on training the neural network
 218 is relatively small. Thus, while the number of records is small, the MeSO-net network is
 219 actually predestined to improve the quality of interpolated values in this region. We may

220 observe more significant changes in the validation stations on validation events combination
 221 by using a more temporal dense network, eg.the Kyoshin Network (K-net), (NIED 2019).

222 We also try to understand the effect on the uncertainty in prediction when another
 223 seismological networks are integrated to the training dataset. Lilienkamp et al. (2022) used
 224 $\hat{\Sigma}$ (given in equation 2) as a proxy for the scatter in observations at station locations, as
 225 it is what we learn with the neural network, and it is supposed to have learned the scatter
 226 in observations and verified its reliability by comparing the distribution of the standardized
 227 residuals, $\tilde{\Delta}$, with the standard normal distribution. The residuals are standardized by
 228 dividing each individual residual by its predicted standard deviation, $\hat{\Sigma}$. We calculated the
 229 $\tilde{\Delta}$ achieved using only the KiK-net data and also together with the MeSO-net dataset for
 230 training. Once this is achieved we compare it with the target normal distribution to analyse
 231 the difference in both distributions (Figure 5). We get a similar standard deviation of $\tilde{\Delta}$
 in both cases, i.e around 14-15 % decrease than the targeted value. Since, we standardized

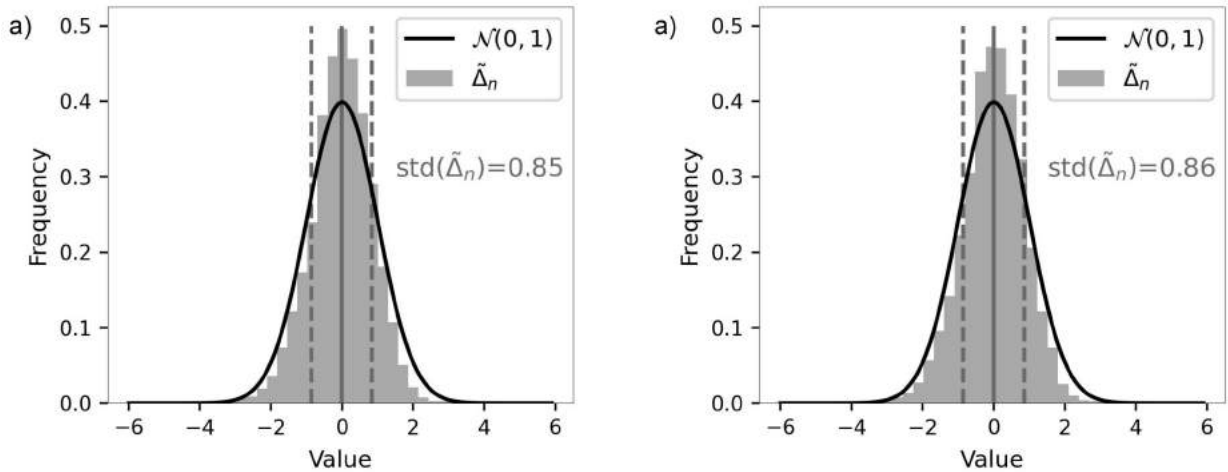


Figure 5: Comparison of the distribution of standardized residuals with the targeted standard normal distribution. Solid and dashed vertical lines indicate the empirical mean and standard deviation (std) of standardized residual, $\tilde{\Delta}$ respectively. a) Training with only KiK-net b) Training with both KiK-net and MeSO-net dataset.

232

233 the residuals by dividing it by the $\hat{\Sigma}$, this standard deviation of 0.86 corresponds to an

234 overestimation of the uncertainty in predictions.

235 We calculate the $\hat{\Delta}$ distribution between all observations from both training and
 236 validation events with respect to the partial ensemble estimators discussed above. All the
 237 four combinations are analysed with respect to the standard Gaussian distribution as shown
 238 in Figure 5 and 6.

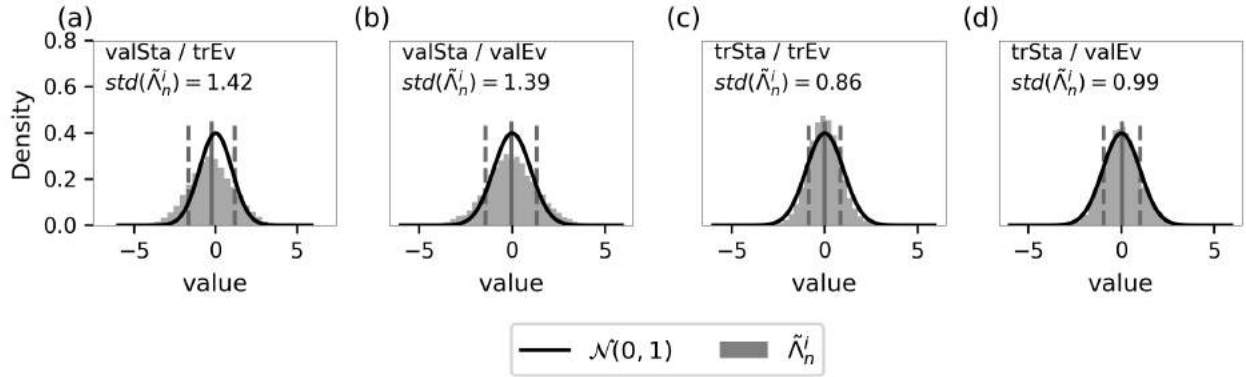


Figure 6: Comparison of the distribution of the standardized residuals with the targeted standard Gaussian distribution for the partial ensemble estimators in all four configurations using the KiK-net dataset.

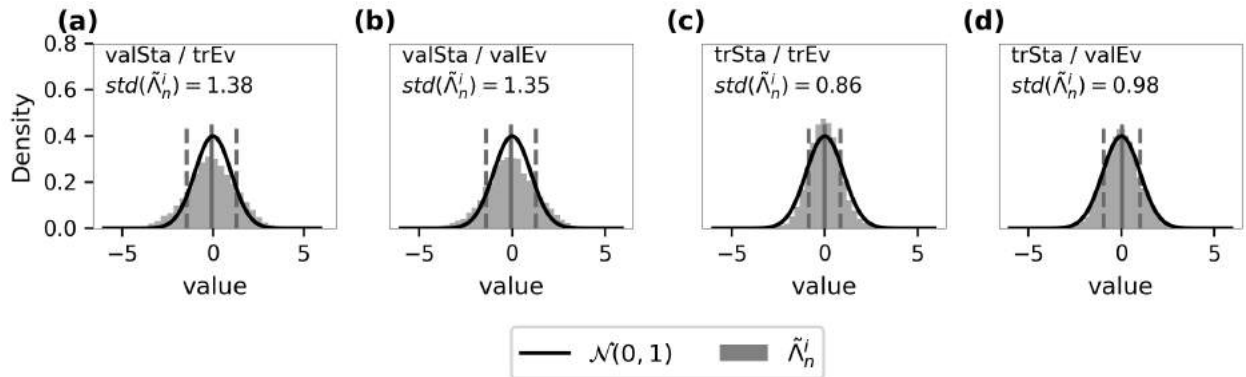


Figure 7: Comparison of the distribution of the standardized residuals with the targeted standard Gaussian distribution for the partial ensemble estimators in all four configurations using both the KiK-net and MeSO-net dataset.

239 The panels (c) and (d) in both figures gives the closest fit to the standard normal
 240 distribution and hence, we can understand that the predictive uncertainty at the training

241 stations are reliable. But while considering the other two panels of both figures, underes-
242 timation of the predictive uncertainty is quite significant - as both are much higher than 1
243 (around 40%). However, the overestimation seems to decrease when an additional network
244 is integrated to the KiK-net dataset. The standard deviation of the validation stations on
245 validation events decreased from 1.39 to 1.35 and the validation stations on training events
246 moved closer to 1 when MeSO-net is added to the U-Net training. These results indicate that
247 the increase in spatial density may contribute to a slight decrease in the underestimation of
248 the predicted standard deviation in the interpolated sites.

249 **5.2 Site amplification**

250 We also analysed the effect of a spatially dense seismological network in the site
251 amplification learned by the U-net architecture. The site specific effects are calculated by
252 training another GMM without using the predictive parameters x_S , y_s and $z_{bedrock}$. We
253 then approximate the site amplification \hat{A}_{mps} learned by subtracting the GMM predictions
254 with and without the site specific predictive parameters. This will provide us with the site
255 amplification maps shown in Figure 7.

256 The maps are plotted for the models trained with only KiK-net and also trained with
257 both KiK-net and MeSO-net. Both the maps behave very similar to each other and there
258 is no significant effect on adding more station data. This may again lead to the fact that
259 both spatially and temporally dense networks are required in understanding the detail and
260 reliable effects.

261 When the map (only using KiK-net) is compared with the amplification maps at SA
262 1s (Figure 8), significant deamplification can be observed. This may be because of the use of
263 $z_{bedrock}$ as the predictive parameter for site and hence, this may indicate that the sediments
264 in the basin are damping high frequencies. More studies are required to understand the
265 difference in site amplification in different frequencies.

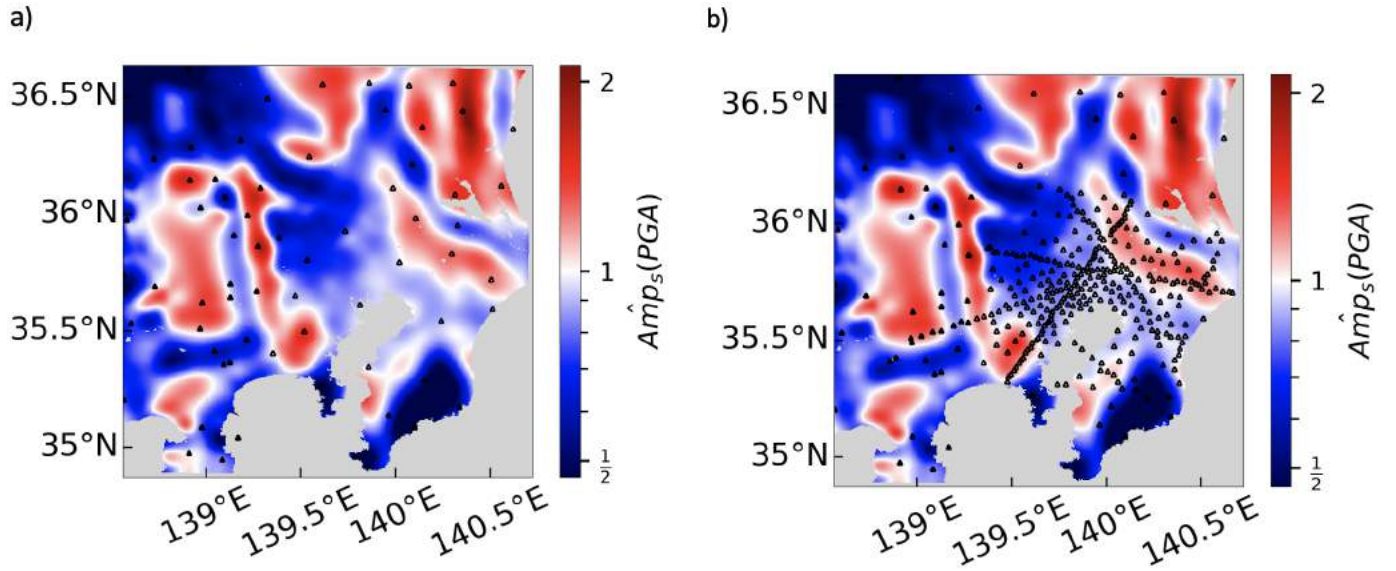


Figure 8: Site amplification estimation of PGA in the Kanto basin approximated from averaged mean predictions. a) KiK-net b) KiK-net + MeSO-net. The black triangles indicate the station locations

266 6 Conclusion and Future work

267 The importance of spatial density in predicting ground motion IMs using the method
 268 developed recently by Lilienkamp et al. (2022) for several applications, including probabilistic
 269 seismic hazard analysis, has been discussed in this deliverable. We here assessed and discussed
 270 the difference in the uncertainty of U-Net’s interpolation of IMs between station locations
 271 when data from multiple networks rather than a single network is used. The operation of
 272 the U-net architecture is studied, and the U-net is trained using only the KiK-net dataset as
 273 well as both the KiK-net and MeSO-net databases. The KiK-net stations have an average
 274 inter-station distance of 94 km and 65 stations are located within our study region, ie the
 275 Kanto basin. The MeSo-net network is much denser than the KiK-net, with an average
 276 inter-station distance of 2-3 km and 300 observation stations located entirely within the
 277 Kanto basin, hence the difference of considering a high dense network in training can be
 278 understood.

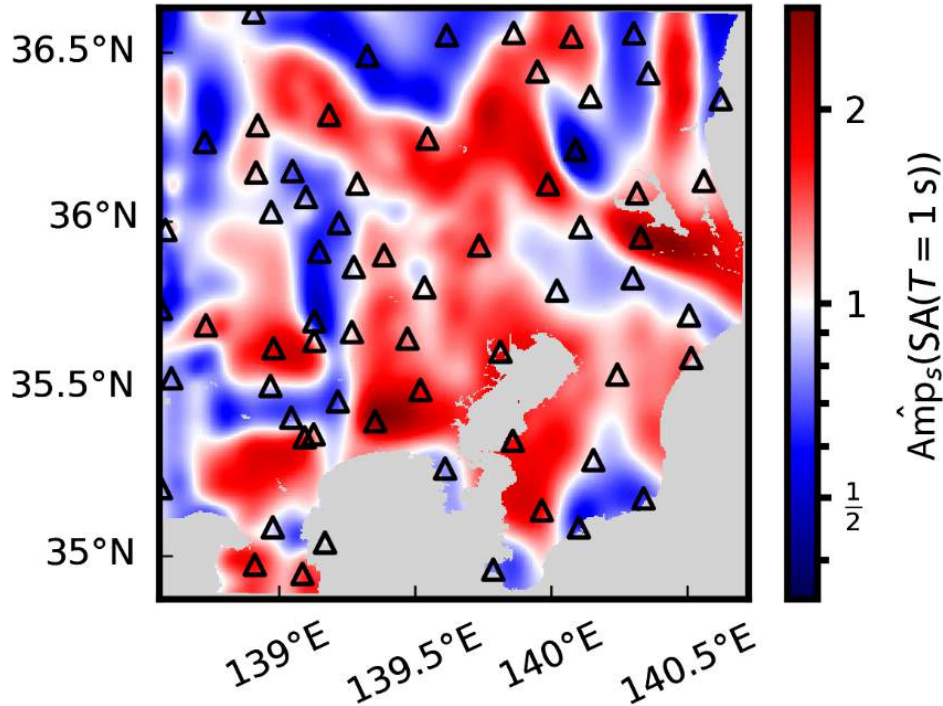


Figure 9: Site amplification estimation of PSA at 1s in the Kanto basin approximated from averaged mean predictions using the KiK-net data. The black triangles indicate the station locations

279 The U-net is trained using a single network and by integrating two networks within the
 280 same region while the validation stations remain the same. The partial ensemble predictions
 281 are analysed to understand the difference of prediction with and without including the MeSO-
 282 net. The rmse values between the observations and predictions of the partial ensemble
 283 estimators decreased after considering the dense network for training. The highest decrease
 284 in the rmse is found on the category of validation stations on validation events, which
 285 shows the effect of the new integrated network on the interpolation of U-Net, however the
 286 significance is still questionable as it is within the standard deviation. More dense networks
 287 are required to understand the significance of the decrease in the rmse values. We then
 288 compared the standardized residual distribution to analyse the accuracy of the predicted
 289 standard deviation. If the standard deviation is less than 1, it corresponds to overestimation
 290 of the uncertainty and vice-versa. Both the results show an overestimation of uncertainty by

291 14-15 %, however when we analysed the partial ensemble estimators the uncertainty range
292 seems to decrease slightly and move towards one when both the datasets are used instead
293 of only KiK-net. Although we integrated a spatially dense network along with the KiK-
294 net dataset to compare the results, more networks with data quantity in both spatial and
295 temporal scale is required to analyse and validate our results.

296 According to the results provided in this report, the error and the uncertainty tends
297 to reduce with the integration of a spatially dense network, however more studies on the
298 changes of IMs with spatial density is required. The site amplification in different frequen-
299 cies is needed to be analysed and investigated using different seismological networks. The
300 availability of the K-net data in the Kanto basin adds an advantage of another network
301 availability within the same region. Integration of K-net along with the KiK-net and the
302 MeSO-net will definitely improve the clarity of the results given in this report. Also, we have
303 analysed the PGA values here, but it will be also more interesting and useful to examine the
304 effect of integration of stations in higher periods PSA ($T = 1s$) because of its probabilistic
305 seismic hazard analysis applications.

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